

Standard Model Problem Set

January 15th, 2025

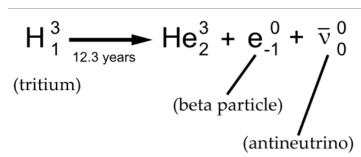


1. Beta Decay

Beta decay is a radioactive process where a neutron in a nucleus is converted to a proton, releasing an antineutrino and an electron (beta-minus decay), or a proton is converted into a neutron, releasing a neutrino and a positron (beta-plus decay). This occurs when a nucleus has too many protons or neutrons to be stable and is caused by the weak interaction.

The neutrino was suggested by Pauli in 1931 as a way to explain the conservation of mass-energy, linear, and angular momentum in beta decay. However, it was only observed and verified in 1956.

- (a) Write the complete nuclear equations for the types of beta decay. Examples:

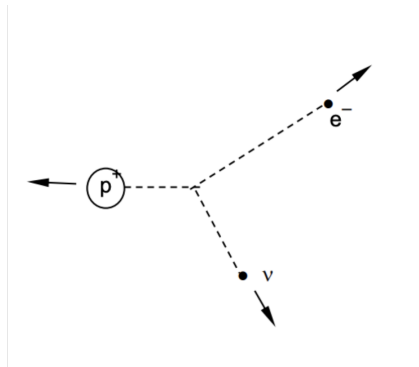


- i. Beta-minus decay of Actinium-230.

- ii. Beta-plus decay of Neptunium-234.

iii. Beta-minus decay of Calcium-45.

- (b) Consider a neutron at rest decaying into a proton, electron, and antineutrino as shown below. The electron is moving at a 30 degree angle to the horizontal at 1.30×10^6 m/s and the proton is moving at 4.5×10^3 m/s.. Neutrinos can have varying levels of energy in beta decay depending on how much of the released energy goes to the beta particle. What is the momentum of the neutrino, and what is its angle to the horizontal? Assume the neutrino has zero mass (this is not accurate).



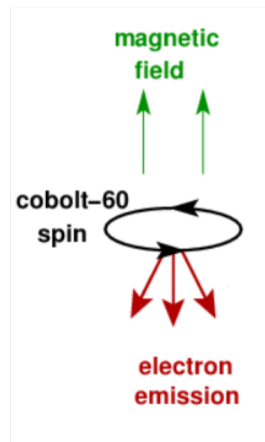
Some helpful constants:

- Mass of a proton: 1.67×10^{-27} kg,
- Mass of an electron: 9.11×10^{-31} kg,

3. Parity Violation

Imagine you're looking in a mirror. The reflection of your right hand looks like a left hand in the mirror, but everything else appears to behave the same way. Parity is the idea that the laws of physics should work the same way in this "mirror image" world. Scientists used to believe this was true for all forces of nature—until the cobalt-60 experiment proved otherwise.

In this experiment, scientists studied a type of radioactive atom called cobalt-60. These atoms decay by releasing electrons. The cobalt-60 nuclei were cooled and placed in a magnetic field, which caused the atoms to align in a specific way, like all spinning tops pointing in one direction (spins are polarized). These atoms are emitted along the negative z direction.



If you were to flip the atom's polarized spin and hence flip the direction of the tops spinning, what direction would you expect the emitted electrons to go? The answer might surprise you!